

# Computational Hypersonics Research at The University of Queensland

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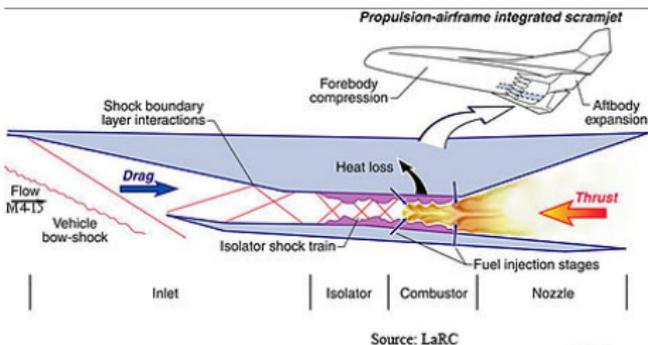
Rowan J. Gollan

8 June 2018

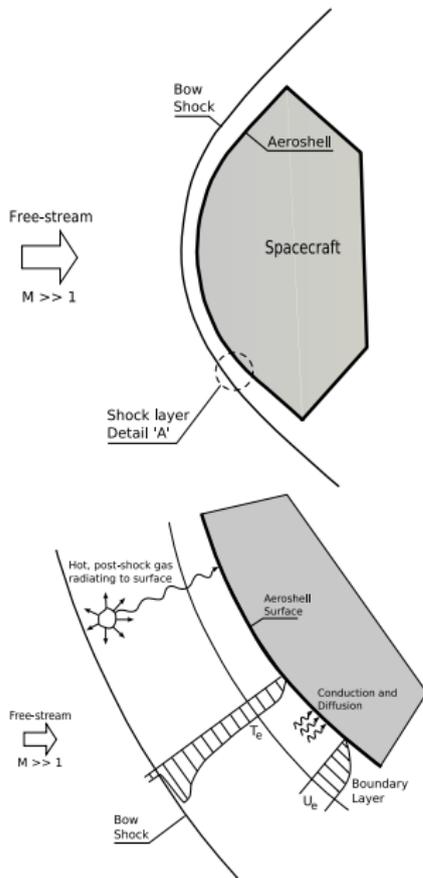
from The University of Queensland presenting at The University of Strathclyde

- Hypersonics research: why and how
- Computational Fluid Dynamics for hypersonic flows
- Eilmer: compressible flow simulator
  - implementation
  - features
- Verification and validation
- New developments
  - shock-fitting mode and moving grids
  - GPU acceleration for reacting flows
  - adjoint-based optimisation

# Why hypersonics?



# Why computer simulation of hypersonic flows?



- The flow physics are modelled reasonably well, but the interactions are complex.
- Physical experimentation provides insights but has limitations, such as: scaling (time and length), boundary conditions, quantification of uncertainties, expense
- Computer simulation complements physical experiments, and vice versa.
- Analysis via computer simulation (might) substitute when we don't have suitable experience.
- Computer analysis good for 'what-if' studies, and design.

# How hypersonics?

Conservation of mass:

$$\frac{\partial}{\partial t} \rho + \nabla \cdot \rho \mathbf{u} = 0 \quad (1)$$

Conservation of species mass:

$$\frac{\partial}{\partial t} \rho_i + \nabla \cdot \rho_i \mathbf{u} = -(\nabla \cdot \mathbf{J}_i) + \dot{\omega}_i \quad (2)$$

Conservation of momentum:

$$\frac{\partial}{\partial t} \rho \mathbf{u} + \nabla \cdot \rho \mathbf{u} \mathbf{u} = -\nabla p - \nabla \cdot \left\{ -\mu(\nabla \mathbf{u} + (\nabla \mathbf{u})^\dagger) + \frac{2}{3} \mu(\nabla \cdot \mathbf{u}) \boldsymbol{\delta} \right\} \quad (3)$$

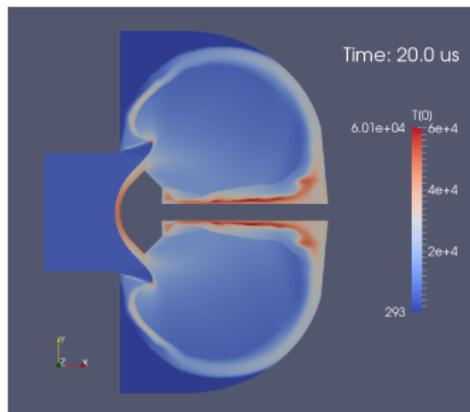
Conservation of total energy:

$$\begin{aligned} \frac{\partial}{\partial t} \rho E + \nabla \cdot \left( e + \frac{p}{\rho} \right) \mathbf{u} = & \nabla \cdot \left[ k \nabla T + \sum_{s=1}^{N_v} k_{v,s} \nabla T_{v,s} \right] + \nabla \cdot \left[ \sum_{i=1}^{N_s} h_i \mathbf{J}_i \right] \\ & - \left( \nabla \cdot \left[ \left\{ -\mu(\nabla \mathbf{u} + (\nabla \mathbf{u})^\dagger) + \frac{2}{3} \mu(\nabla \cdot \mathbf{u}) \boldsymbol{\delta} \right\} \cdot \mathbf{u} \right] \right) - Q_{\text{rad}} \quad (4) \end{aligned}$$

Conservation of vibrational energy:

$$\frac{\partial}{\partial t} \rho_i e_{v,i} + \nabla \cdot \rho_i e_{v,i} \mathbf{u} = \nabla \cdot [k_{v,i} \nabla T_{v,i}] - \nabla \cdot \mathbf{e}_{v,i} \mathbf{J}_i + Q_{T-v_i} + Q_{V-v_i} + Q_{\text{Chem}-v_i} - Q_{\text{rad},i} \quad (5)$$

## Eilmer features – 1/2



- 2D/3D compressible flow simulation.
  - Gas models include ideal, thermally perfect, equilibrium.
  - Finite-rate chemistry.
  - Multi-temperature and state-specific thermochemistry.
  - Inviscid, laminar, turbulent ( $k-\omega$ ) flow.
- Solid domains with conjugate heat transfer in 2D.
  - User-controlled moving grid capability, with shock-fitting method for 2D geometries.
  - Dense-gas thermodynamic models and rotating frames of reference for turbomachine modelling.

## Eilmer features – 2/2



- Transient, time-accurate, using explicit Euler, PC, RK updates.
  - Alternate steady-state solver with implicit updates using Newton-Krylov method.
  - Parallel computation via shared-memory on workstations, and using MPI on a cluster computer.
  - Multiple block, structured and unstructured grids.
  - Native grid generation and import capability.
  - Unstructured-mesh partitioning via Metis.
- 
- [en.wikipedia.org/wiki/Eilmer\\_of\\_Malmesbury](http://en.wikipedia.org/wiki/Eilmer_of_Malmesbury)
  - Gas model calculator and compressible flow relations.

## Origins

- in the late 1980s, the state of the art for scramjet simulations involving reactive flow was JP Drummond *SPARK* code
- Flow solver component based on Bob McCormack's (1969) finite-difference shock-capturing technique.
- All configuration hard-coded into the Fortran source code and compiled to run on a Cray supercomputer.
- In the 1980s, a new CFD technology (upwind flux) was being developed by the applied mathematics people and parallel computing environments were being developed by the computer science people (cluster computers).
- Dec 1990: following a CFD lesson on the chalk-board from Bob Walters and Bernard Grossman, *cns4u* was started with the intention to be like *SPARK* but with new technology

## Development of Eilmer

- 1993 built *sm3d*, a space-marching code for 3D scramjet flows
- 1995 through 1999: the postgrad years expanded scope of experimentation and application
- 1996: code reformulation around fluxes (frequent discussions with Mike Macrossan); all code still in C with a preprocessor having a little command interpreter built in.
- 1997: discovered scripting languages Tcl and Python
- May 2003: *scriptit.tcl* provided fully programmable environment for simulation-preparation.
- Aug 2004: *Elmer* began as a hybrid code using Python and C.
- Jun 2005: rewrite of *Elmer(2)* in C alone.
- Jul 2006: rewrite *Elmer2* in C++ and, in 2008, call it *Eilmer3*. Class-based implementation was easier to extend.

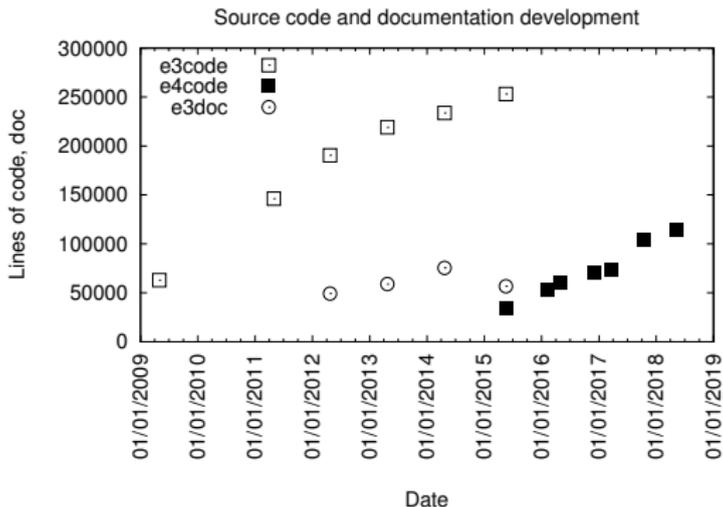
## Eilmer4 – think big, but control the complexity



- Jun 2015+: rebuild in the D and Lua programming languages.
- Heather Muir worked on the unstructured-grid generator. based on the paving algorithm.

# Implementation

D language data storage and solver, with embedded Lua interpreters for preprocessing, user-controlled run-time configuration in boundary conditions and source terms and thermochemical configuration.



At 60 lines per page, the Eilmer4 code is equivalent to a 1200 page document.

# Verification & Validation

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## Quality Control: Verification & Validation

To quote Blottner:

*Verification: are we solving the equations right?*

*Validation: are we solving the right equations?*

Verification:

- comparison to exact solutions
- comparison to manufactured solutions
- order of accuracy test
- code-to-code comparison

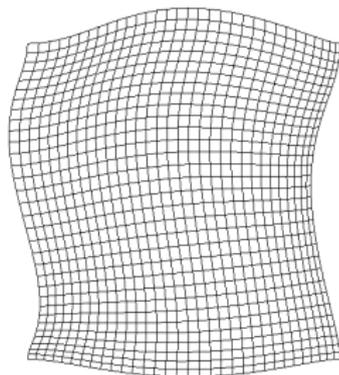
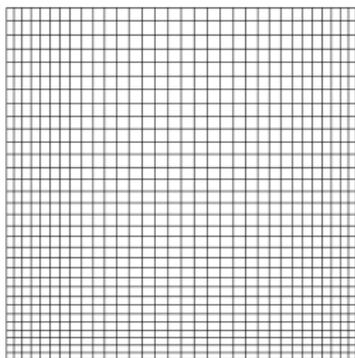
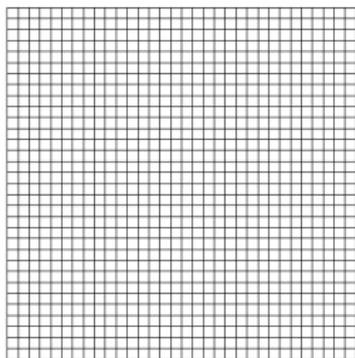
Validation:

- are our models of flow physics correct
- comparison to experimental measurements

## Verification for inviscid flows

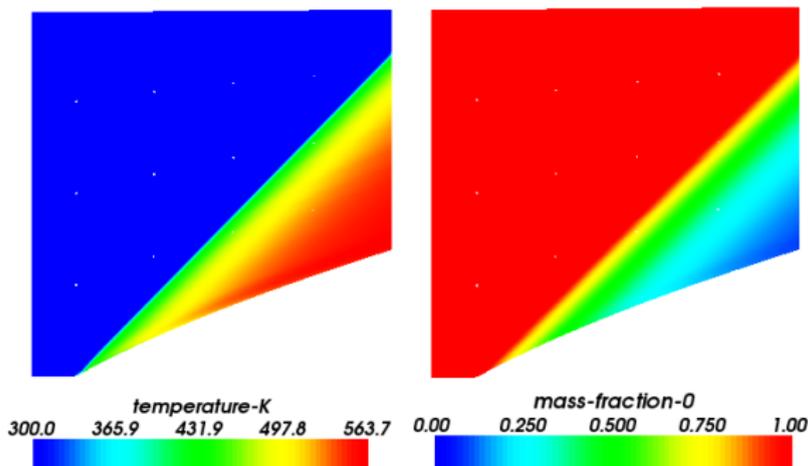
For inviscid flows, we have verified the code using:

- Roy's manufactured solution for supersonic inviscid flow.  
Demonstrated 2nd order spatial accuracy on regular, stretched, and distorted grids.
- Power & Stewart's exact solution for an oblique detonation wave.  
Demonstrated 1st order spatial accuracy in the presence of shocks.



## Verification: oblique detonation wave

The flow problem is an oblique detonation wave which is supported by a curved wedge surface. The analytical solution for this problem was first presented by Powers & Stewart (AIAA J. 1992), and first employed for verification by Powers & Aslam (AIAA J. 2006).



In order to make the problem analytically tractable, the reaction mechanism for the detonation is simplified. The reaction is a one-step reaction that proceeds once an ignition temperature is reached.

## The Powers and Aslam gas model

- Two species A, B, with reaction of A to B proceeding at rate

$$\frac{d\rho_B}{dt} = \alpha \rho_A H(T - T_i)$$

with rate constant  $\alpha = 0.001 \text{ s}^{-1}$

- Reaction progress variable is mass fraction of B:  $\lambda = Y_B = \frac{\rho_B}{\rho}$
- $Y_A = 1 - Y_B$
- Equation of state for internal energy:

$$u = \frac{1}{\gamma - 1} \frac{p}{\rho} - \lambda q = C_v T - Y_B q$$

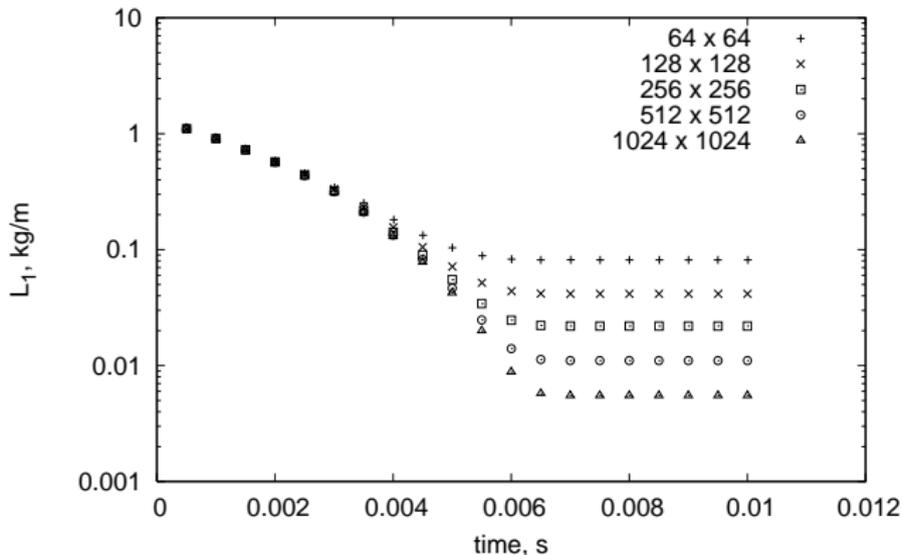
with heat of reaction  $q = 300000 \text{ J/kg}$  and ratio of specific heats  $\gamma = 6/5$ .

- Pressure:  $p = \rho RT$ , with gas constant  $R = 287 \text{ J/kg.K}$

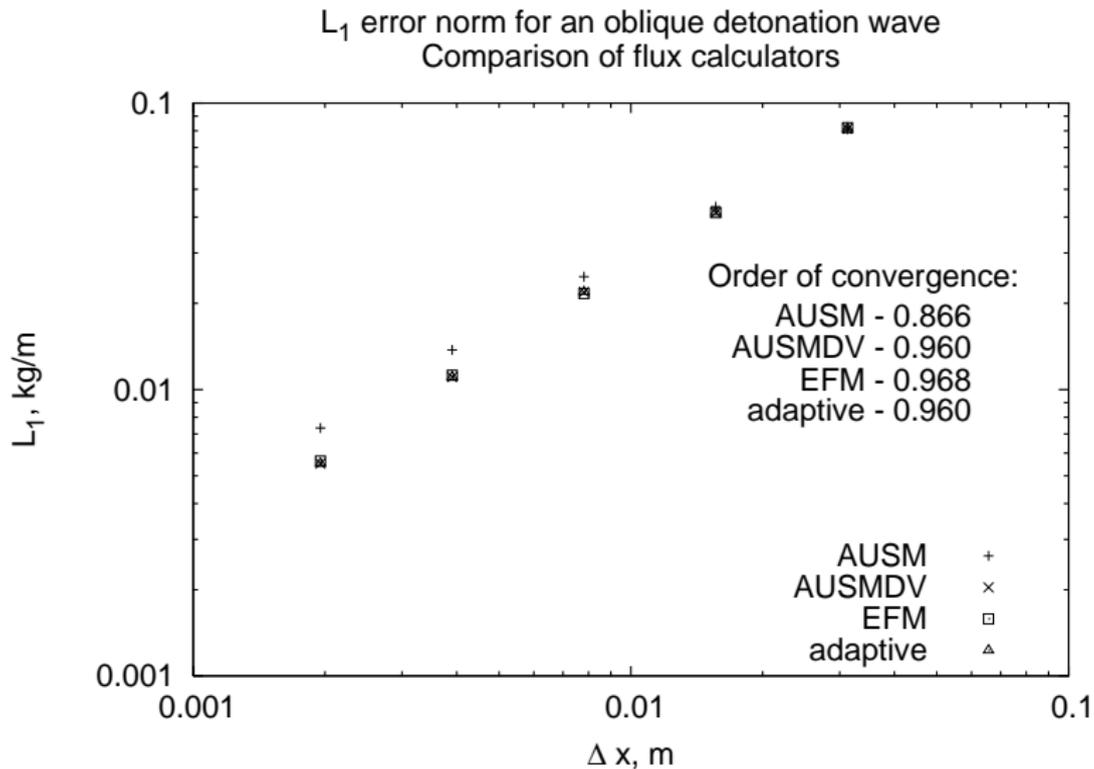
# Oblique detonation wave results – 1/2

$$L_1 = \sum_{i=1}^{N_i} \sum_{j=1}^{N_j} |\rho_{n,ij} - \rho_{e,ij}| \Delta x \Delta y$$

$L_1$  error norm for an oblique detonation wave  
AUSMDV flux calculator



## Oblique detonation wave results – 2/2



## Flows with chemical nonequilibrium

- Flow can be distinguished (and modelled) in three classifications:
  - frozen flow (ideal gas model) –  $t_{chem} \gg t_{flow}$
  - nonequilibrium flow (finite-rate chemistry) –  $t_{chem} \approx t_{flow}$
  - equilibrium flow –  $t_{chem} \ll t_{flow}$
- Model for rate of chemical change: Law of Mass Action

$$\frac{d[X_i]}{dt} = (\nu_i'' - \nu_i') \left\{ k_f \prod_i [X_i]^{\nu_i'} - k_b \prod_i [X_i]^{\nu_i''} \right\}$$

- Forward and reverse rates are computed from a modified Arrhenius form

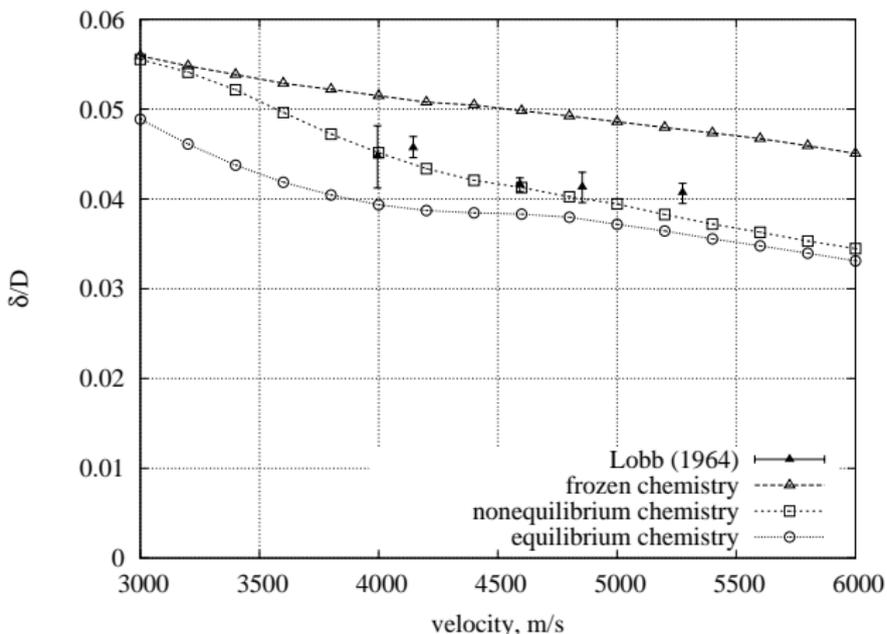
$$k = AT^n e^{-T_a/T}$$

alternatively, reverse rates may come from computing the equilibrium constant

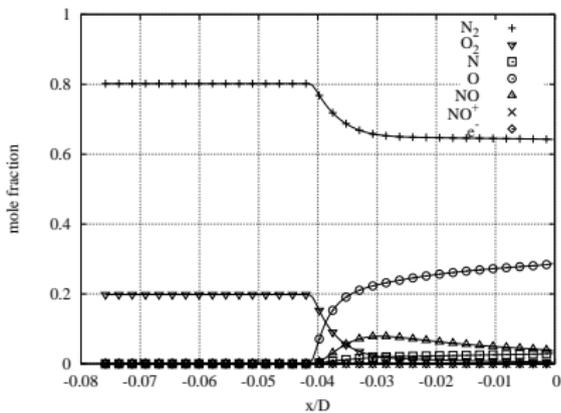
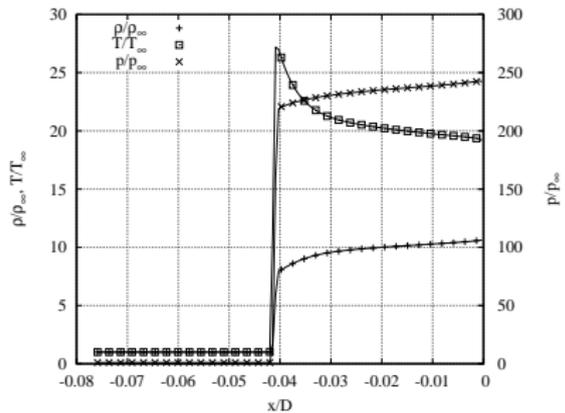
- This ODE integrators available are:
  - Mott's  $\alpha$  Quasi-Steady-State approach (for stiff systems, eg. combustion)
  - Runge-Kutta-Fehlberg (efficient for non-stiff systems, eg. endothermic chemistry)

# Validation of reacting flow model for air

- Lobb (1964) performed a series of experiments to measure shock detachment distance on spheres fired into air at hypervelocities
- A 0.5 in nylon sphere was fired in a ballistic range into air at various speeds and pressures



# Stagnation streamline properties for reacting air over sphere



# Flows with thermal nonequilibrium

molecules:

translation

rotation

vibration

electronic

atoms:

translation

electronic

*Why isn't the vibrational energy in equilibrium?*

- it typically takes 5-10 collisions for the rotational mode to equilibrate at the translational temperature
- however, it can take on the order of  $10^2$ - $10^3$  collisions for vibrational modes to equilibrate

*A specific example...*

For a blunt body of nose radius 1 m with a velocity of 10 km/s at an altitude of 75 km:

$$\tau_{flow} \approx 10^{-4} s, \tau_{chem} \approx 10^{-3} s, \tau_{vib} \approx 10^{-5}$$

## Engineering model for flows with thermal nonequilibrium

$$\frac{\partial}{\partial t} \rho_i e_{v,i} + \nabla \cdot \rho_i e_{v,i} \mathbf{u} = \nabla \cdot [k_{v,i} \nabla T_{v,i}] - \nabla \cdot \mathbf{e}_{v,i} \mathbf{J}_i + Q_{T-v_i} + Q_{V-v_i} + Q_{\text{Chem}-v_i} - Q_{\text{rad},i}$$

- Internal energy modes are separable (Born-Oppenheimer approximation)
- Each separated mode is assumed to populate a Boltzmann distribution at a particular temperature
- Nonequilibrium occurs when these governing temperatures differ for different energy modes
- Depending on extent of nonequilibrium, each molecular species might have its own describing vibrational temperature
- Example: four-temperature air model has one temperature to describe translational/rotational energy and one temperature each for vibrational energy of  $\text{N}_2$ ,  $\text{O}_2$  and  $\text{NO}$

## Thermal nonequilibrium: energy exchange

$$\frac{\partial}{\partial t} \rho_i e_{v,i} + \nabla \cdot \rho_i e_{v,i} \mathbf{u} = \nabla \cdot [k_{v,i} \nabla T_{v,i}] - \nabla \cdot e_{v,i} \mathbf{J}_i + Q_{T-v_i} + Q_{V-v_i} + Q_{\text{Chem}-v_i} - Q_{\text{rad},i}$$

*Translational-vibrational energy exchange*

$$Q_{T-v_i} = \sum_{c=1}^{n_s} x_c \frac{e_{v,p}^* - e_{v,p}}{(T_V^{p-c})_{V-T}}$$

*Vibrational-vibrational energy exchange*

$$Q_{V-v_i} = \sum_{q=1, q \neq p}^{n_v} \frac{x_q}{(T_V^{p-q})_{V-V}} \left( \frac{1 - \exp(-\Theta_{v,p}/T)}{1 - \exp(-\Theta_{v,q}/T)} \frac{e_{v,q}}{\hat{e}_{v,q}} (\bar{e}_{v,p} - e_{v,p}) - \frac{e_{v,p}}{\hat{e}_{v,q}} (\bar{e}_{v,q} - e_{v,q}) \right)$$

## Thermal nonequilibrium: chemistry-energy coupling

$$\frac{\partial}{\partial t} \rho_i e_{v,i} + \nabla \cdot \rho_i e_{v,i} \mathbf{u} = \nabla \cdot [k_{v,i} \nabla T_{v,i}] - \nabla \cdot e_{v,i} \mathbf{J}_i + Q_{T-v_i} + Q_{v-v_i} + Q_{\text{Chem}-v_i} - Q_{\text{rad},i}$$

### Chemistry-vibration coupling

- If the gas is in nonequilibrium, how are the reaction rates affected?

$$k = k^{EQ}(T) \Psi(T, T_{v,i})$$

- When chemical reactions take place, how does this effect the average vibrational energy?
- A preferential model is implemented in Eilmer by Knab et al. This is a generalised and extended version of Treanor & Marrone's preferential dissociation model.

$$Q_{\text{Chem}-v_i} = \sum_{j=1}^{Nr} \left[ -G_{va,ij} \frac{1}{f_i} \left( \frac{df_j}{dt} \right)_f + G_{app,ij} \frac{1}{f_i} \left( \frac{df_j}{dt} \right)_r \right]$$

# Validation: 2-temperature reacting air flow over a sphere

Nonaka experiment:

$vel.x = 3490 \text{ m/s}$

$p_{inf} = 4850 \text{ Pa}$

$T_{inf} = 293 \text{ K}$

$f_{N2} = 0.767$

$f_{O2} = 0.233$

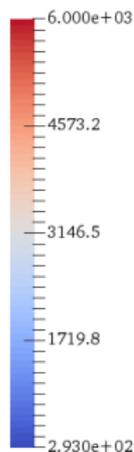


$t = 60.172 \text{ micro s}$

Top half: translational temperature

Bottom half: vibroelectronic temperature

temperature, K



Model:

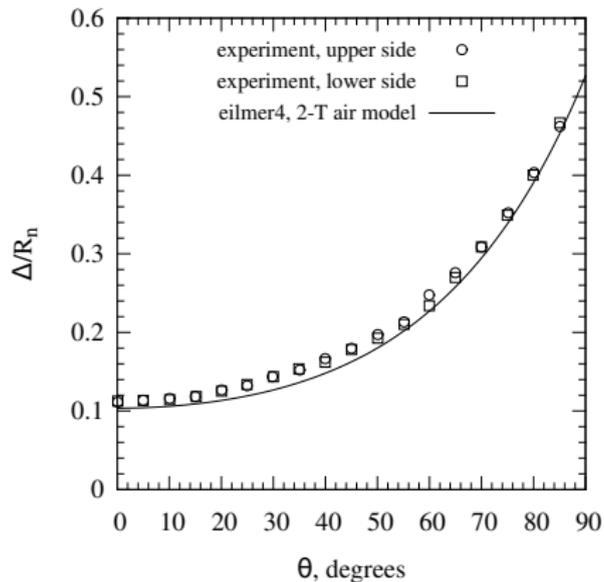
5-species, 2-temperature air

Gupta et al reaction rates

Park 2-T modifications for rate constants

# Validation: 2-temperature reacting air flow over a sphere

Shock shape in front of a sphere fired in air  
 $R_n = 7.0\text{mm}$ ,  $u_\infty = 3.49\text{ km/s}$ ,  $p_\infty = 4850\text{ Pa}$ ,  $\rho_\infty R_n = 4.0\text{e-}4\text{ kg/m}^2$



## **Recent Development Activity**

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## Recent Development Activity

Advanced and experimental features:

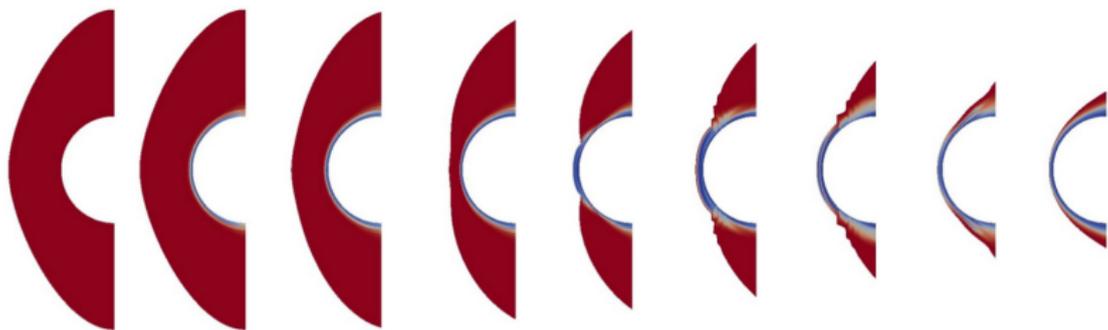
- user customisation/control of boundary conditions, source terms and grid motion via Lua scripts
- moving grids
- shock-fitting boundaries
- wall models for RANS simulations
- GPU-acceleration for reacting flows
- coupled fluid/solid domains for conjugate heat transfer problems
- steady-solver using Newton-Krylov method
- adjoint solver for CFD-in-the-loop optimisation

## Moving grid capability

- Moving grids and moving boundaries are also controlled using small Lua programs built by the user.
- It is hard to predict all the types of motion that users would want to simulate, hence the user-built programs to control the motion.
- The user needs to set the velocity of the grid points and the simulation code takes care of updating to the new positions.
- With enough creativity, this can be used to simulate fluid-structure interaction problems.

## Shock-fitting boundaries

- For blunt body flows, it is critical to have nicely aligned grids with the bow shock.
- One solution is to do direct shock-fitting at the boundaries.
- Eilmer uses moving grid capability and a specialised shock-fitting boundary condition to allow shock-fitting at inflow boundaries.



# GPU acceleration for chemically reacting flows

## Graphics Processing Units for High Performance Computing



CPUs:

- + excellent serial thread performance
- + modern branch prediction and efficient memory access
- + handle complex algorithms well without too much developer intervention

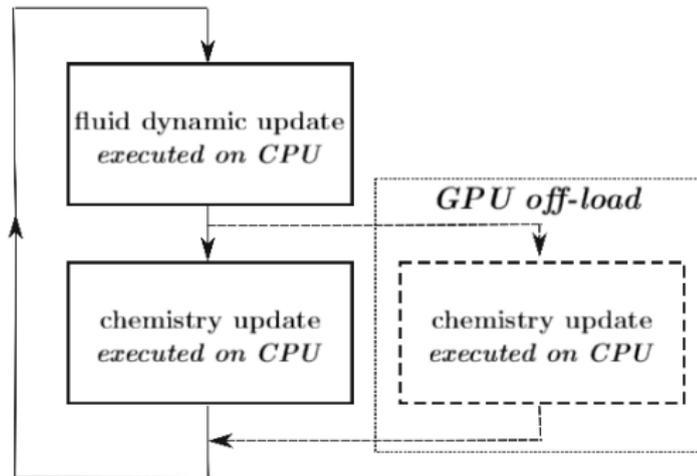


GPUs:

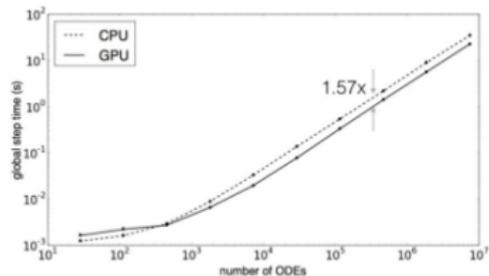
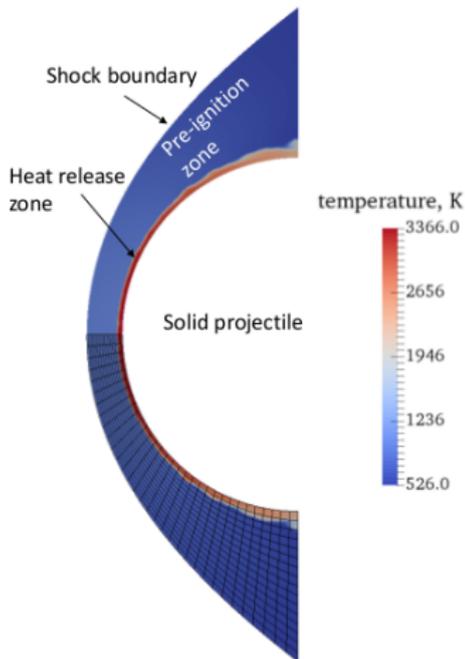
- + excel at floating point operations
- + high performance through thread parallelism
- + parallelism is Single-Instruction, Multiple-Data (SIMD) type
- + hardware abstraction is low: requires careful effort on part of developer

# GPU acceleration: Eilmer implementation

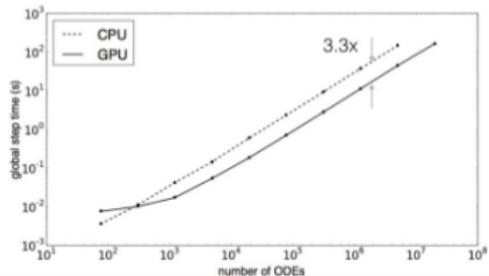
+ operator-splitting algorithm



# GPU acceleration: proof-of-concept, early results



Hydrogen combustion



Methane combustion

Website:

`cfcfd.mechmining.uq.edu.au/eilmer`

Source code repository:

`bitbucket.org/cfcfd/dgd`

Documentation in the Eilmer 4.0 guides:

- *Guide to the transient flow solver*
- *Guide to the basic gas models package*
- *Guide to the geometry package*
- *Formulation of the transient flow solver*
- *Reacting gas thermochemistry*